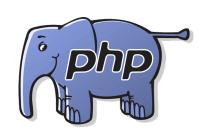
CS 360 Programming Languages Day 8



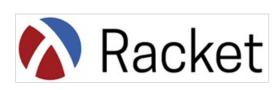




















Review

- A first-class citizen is a data type that can be
 - Passed as an argument to a function.
 - Returned as a value from a function.
 - Assigned to a variable.
 - (Stored in a data structure.)
 - (Created at run-time [dynamically, on-the-fly])
- First three are always part of the definition; last two sometimes.

Review

• Lambda expression: creates and returns an *anonymous function*.

```
(lambda (arg1 arg2 ...) expression)
```

Term comes from the lambda calculus.

- Developed by Alonzo Church.
- A formal way of studying the properties of computation, like Turing machines.



Review

- Higher order functions:
 - Take functions as arguments, or
 - Return functions.
- Map and filter both take functions as arguments.
 - Map: Applies a function to every (top-level) item within a list.
 (map func 1st)
 - Filter: Takes a list L and a predicate P; returns a list of all the values in L that satisfy P.

```
(filter pred 1st)
```

Map examples

```
(define (map func 1st)
 (if (null? lst) '()
      (cons (func (car lst)) (map func (cdr lst)))))
(define (double x) (* x 2))
(map\ double\ '(1\ 2\ 3)) => '(2\ 4\ 6)
(map (lambda (x) (* x 2)) '(1 2 3)) => '(2 4 6)
(map car '((1 2 3) (4 5) (6) (7 8 9))) => '(1 4 6 7)
(define (scale factor 1st)
  (map (lambda (x) (* x factor)) lst)
(scale 2 '(1 2 3)) => '(2 4 6)
```

Map examples

```
(map (lambda (x) (+ x 1)) '(1 2 3)) => ?
(map (lambda (x) (cons x '()) '(1 2 3)) => ?
(map (lambda (x) (list x)) '(1 2 3)) => ?
(map (lambda (x) (if (> x 0) (* x 2) (* x 3))) '(1 -2 -3 4))
```

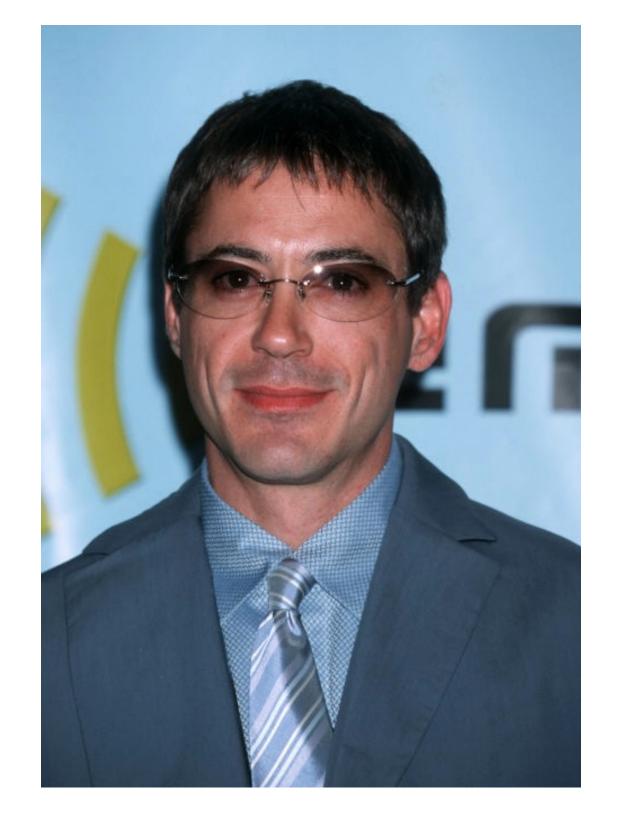
Key to using map with lambda expression: the argument to the lambda expression (x) represents each element of the list in turn.

Filter examples

```
(define (filter func 1st)
 (cond ((null? lst) '()
        ((func (car lst))
          (cons (func (car lst)) (filter func (cdr lst))))
        (#t
          (filter func (cdr lst)))))
(filter odd? '(1 2 3)) => '(1 3)
(define (keep-odds lst)
  (filter odd? lst)
(filter (lambda (x) (> x 0)) '(-1 2 -3 4)) => '(2 4)
```

Filter examples

```
(filter (lambda (x) (= 1 (remainder x 2))) '(1 2 3)) \Rightarrow?
(define (keep-divisible factor 1st)
  (filter lst))
(filter (lambda (lst) (even? (car lst)))
           '((1 2 3) (4 5) (6 7))) => ?
(filter (lambda (lst) (even? (car lst)))
           '((1 2 3) (4 5) (6 7) ())) => ?
(define (keep-longer-than n 1st)
  (filter ____ lst))
```





- Recall that Racket has a expt function:
 - (expt x y) => x raised to the y power
- We can define a square function like this:

```
(define (square x) (expt x 2))
```

Or a cube function like this:

```
(define (cube x) (expt x 3))
```

- But this gets rather repetitive.
- What if we wanted to create a lot of these "raise to a power" functions?

Functions that return functions!

```
(define (to-the-power exponent)
      (lambda (x) (expt x exponent)))
```



Functions that return functions!

```
(define (to-the-power exponent)
   (lambda (x) (expt x exponent)))
```

Define a function called to-the-power that takes a variable called exponent...

...that returns an anonymous function of a single variable x...

...that raises x to the power of the exponent variable.

How to use this

Old way:

```
- (define (square x) (expt x 2))
- (define (cube x) (expt x 3))
```

New way:

```
- (define square (to-the-power 2))
- (define cube (to-the-power 3))
```

- Notice that the new way doesn't use extra parentheses around the name of the function
 - Don't need 'em: what would we do with the argument?

Another example

```
(define (add3 num) (+ 3 num))(define (add17 num) (+ 17 num))
```

New way:

```
(define (create-add-function inc)
    (lambda (num) (+ inc num)))
(define add3 (create-add-function 3))
(define add17 (create-add-function 17))
```

Getting more complicated

 How about a function that takes functions as arguments and returns a new function?

```
    (define (compose f g)
        (lambda (x) (f (g x))))
    (define second (compose car cdr))
    (define third (compose car (compose cdr cdr)))
    (map third '((2013 5 6) (2012 1 8) (2000 7 7)))
```

Transformations on functions

Imagine you have a function that must take a non-empty list argument:

More families of functions

```
(define (divisible n)
      (lambda (x) (= 0 (remainder x n))))
(define (make-quad-polynomial a b c)
      (lambda (x)
      (+ (* a x x) (* b x) c)))
```

A little syntax

- How to call a function:
 - (f e1 e2 e3...)
 - f is a function name and e1, e2... are expressions that will be evaluated and passed as the values of the arguments to f.
- Turns out f doesn't have to be a function name.
- f can be any expression that evaluates to a function!

A little syntax

- All of these evaluate to a function:
 - the name of a function (e.g., cons, car, +, …)
 - a lambda expression
 - a function call that returns a function



One more abstraction. Compare:

```
(define (length 1st)
 (if (null? lst) 0
    (+ 1 (length (cdr lst)))))
(define (sum-list lst)
 (if (null? lst) 0
    (+ (car lst) (sum-list (cdr lst)))))
(define (map func 1st)
 (if (null? lst) '()
    (cons (func (car lst)) (map func (cdr lst)))))
```

One more abstraction. Compare:

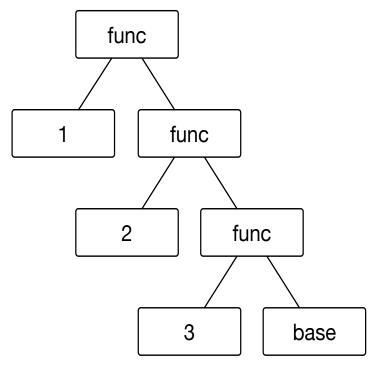
```
(define (length 1st)
 (if (null? 1st) 0
    (+ 1 (length (cdr lst))))
(define (sum-list lst)
 (if (null? lst) 0
    (+ (car lst) (sum-list (cdr lst))))
(define (map func 1st)
 (if (null? lst) '()
    (cons (func (car 1st)) (map func (cdr 1st)))))
```

One function to rule them all



(foldr func base 1st)

Say
$$1st = '(1 2 3)$$



- Foldr applies func repeatedly to pairs of items, starting from the right end of the list.
- The first two items are the last item in the list and the base element.
- The function must be a function of two items.

```
(f 1 (f 2 (f 3 base)))
```

- In general, for 1st = (x1 x2 ... xn)
- (f x1 (f x2 (f x3 (f ... (f xn base)))...)

```
(define (sum-list-new lst)
     (foldr + 0 lst))
(define (length-new lst)
  (foldr
    (lambda (elt cdr-len) (+ 1 cdr-len))
   0 lst))
(define (my-map func lst)
  (foldr
    (lambda (car cdr) (cons (func car) cdr))
    '() lst))
```